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ALL SOLID-STATE RGB AND WHITE LIGHT GENERATOR

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BACKGROUND OF THE INVENTION

The present invention relates generally to devices for generating visible light from a laser. More specifically, but without limitation thereto, the present invention relates to a device for generating red, green, and blue (RGB) light.

SUMMARY OF THE INVENTION

The present invention has applications in the field of color displays, including computer monitors, video games, television, and other applications that may require a variety of light wavelengths.

In one aspect of the invention, a light generator can generate light having selected proportions of red, green, and blue wavelengths from a single source of blue light.

In another aspect of the invention, beamsplitters are used to split the beam of blue light into separate beams to generate light having a single color in each beam. Upconversion lasers may be used to generate each of the single colors. The colors may be red, green, and blue, respectively. The light generator may include a first beamsplitter optically coupled to the blue laser for splitting a second beam of blue light from the first beam of blue light, a second beamsplitter optically coupled to the first beamsplitter for splitting a third beam of blue light from the first beam of blue light, a first upconversion laser optically coupled to the second beamsplitter for generating a beam of green light from the first beam of blue light, and a second upconversion laser optically coupled to the second beamsplitter for generating a beam of red light from the third beam of blue light.

In a further aspect of the invention, beamsplitters are used to split a beam of blue light into separate beams to generate light having one or more colors in each separate beam. In a specific embodiment, one beam may have the colors of red and green. The light generator may include a blue laser for generating a first beam of blue light, a first beamsplitter optically coupled to the blue laser for splitting a second beam of blue light from the first beam of blue light, and an upconversion laser optically coupled to the first beamsplitter for generating a beam of red light and a beam of green light from the first beam of blue light.

In another aspect of the invention, the light generator generates a single collinear beam containing multiple colors from a single beam of blue light. The colors may be red, green, and blue. The light generator may include a blue laser for generating a beam of blue light and an upconversion laser optically coupled to the blue laser for generating a beam of red light and a beam of green light from the beam of blue light.

BRIEF DESCRIPTION OF THE DRAWINGS

The above and other aspects, features and advantages of the present invention will be more apparent from the following more specific description thereof, presented in conjunction with the following drawings wherein:

FIG. 1 is a diagram of a solid-state blue laser for generating blue light in accordance with the prior art;

FIG. 2 is a diagram of a light generator with two upconversion lasers according to an embodiment of the present invention;

FIG. 3 is a diagram of a light generator with a single upconversion laser according to another embodiment of the present invention;

FIG. 4 is a diagram of a light generator for
5 generating collinear beams of red, green, and blue light according to a further embodiment of the present invention; and

FIG. 5 is a diagram of a light generator for generating separate beams of red, green, and blue light
10 and combining the separate beams to form a collinear beam of combined light according to an additional embodiment of the present invention.

Corresponding reference characters indicate corresponding elements throughout the several views of
15 the drawings.

DESCRIPTION OF SOME EMBODIMENTS

The present invention has applications in the field of color displays, including computer monitors,
20 video games, television, and other applications that may require a variety of light wavelengths.

In one aspect of the invention, a light generator can generate light having selected proportions of red, green, and blue wavelengths from a single source
25 of blue light. In a specific embodiment, the light generator includes a blue laser for generating a first beam of blue light.

FIG. 1 is a diagram of a prior art solid-state blue laser 100 for generating blue light. Shown in FIG.
30 1 are a laser diode 102, a focusing lens 104, an input coupler 105, a laser gain element 106, an output coupler 108, a frequency doubler 110, and a beam of blue light 112.

The laser diode 102 may be, for example, an
35 AlGaAs laser emitting light at a wavelength of 808 nm in the near infrared.

The laser diode 102 pumps the laser gain element 106, which may be, for example, a cylindrically shaped Nd:YAG crystal producing a laser wavelength of 946 nm, a length of about 5 mm, and a diameter of about 3 mm.

5 The focusing lens 104 focuses the near infrared pump energy from the laser diode 102 through the input coupler 105 onto the laser gain element 106. The input coupler 105 may be, for example, a plane mirror or a reflective coating on a face of the laser gain element 106 adjacent

10 to the focusing lens 104 that is transmissive at the wavelength of the near infrared pump energy output from the laser diode 102 and is reflective at the laser wavelength of the laser gain element 106.

The output coupler 108 may be, for example, a

15 concave mirror. The output coupler 108 is preferably partially reflective, for example, between 10% and 99% reflective, at the second harmonic of the laser wavelength of the laser gain element 106. The output coupler 108 totally reflects and focuses the light

20 generated by the laser gain element 106 back to the laser gain element 106. The output coupler 108 may also reflect the near infrared pump energy of the laser diode 102 that is not absorbed by the laser gain element 106 back to the laser gain element 106 to increase optical

25 efficiency.

The light generated by the laser gain element 106 is optically coupled to the frequency doubler 110. The frequency doubler 110 may be, for example, a cylindrically shaped beta-barium borate (BBO) crystal

30 with anti-reflective coatings on both end faces that are highly transmissive of the light generated by the laser gain element 106. Typical dimensions for the frequency doubler 110 are 3mm in diameter and 5 mm in length. The frequency doubler 110 converts the fundamental wavelength

35 of light produced by the gain element 106 to the second harmonic to produce the beam of blue light 112. In this

example, the wavelength of the blue light is about 473 nm. The beam of blue light 112 output from the blue laser 100 may be used in conjunction with each of the embodiments described below to construct a solid-state RGB light generator.

FIG. 2 is a diagram of a light generator 200 with two upconversion lasers. Shown in FIG. 2 are a first beam of blue light 112, a first beamsplitter 202, a first mirror 204, a second beam of blue light 206, a second beamsplitter 208, a second mirror 210, a first focusing lens 212, a first input coupler 213, a first upconversion laser gain element 214, a first output coupler 216, a beam of green light 218, a second focusing lens 220, a second input coupler 221, a second upconversion laser gain element 222, a second output coupler 224, a beam of red light 226, and optical modulators 250a, 250b, and 250c.

The first beamsplitter 202 may be a 90%-10% beamsplitter, i.e., 90 percent transmissive, 10 percent reflective. An example of a beamsplitter that may be used for the first beamsplitter 202 that is commercially available from numerous suppliers is a flat quartz plate coated with a dichroic coating. The first beamsplitter 202 reflects about 10% of the first beam of blue light 112 to become the second beam of blue light 206 and directs the second beam of blue light 206 to the first mirror 204.

The first mirror 204 directs the second beam of blue light 206 in a direction approximately parallel to the first beam of blue light 112. The first mirror 204 and the second mirror 210 may be, for example, plane mirrors or internally reflecting prisms.

The second beamsplitter 208 may be a 50%-50% beamsplitter similar in construction to the first beamsplitter 202, however, the composition of the dichroic coating is selected to reflect about 50% of the

first beam of blue light 112 transmitted by the first beamsplitter 202 to the second mirror 210. The second mirror 210 directs the portion of the first beam of blue light 112 reflected by the second beamsplitter 208 to the first focusing lens 212. The first focusing lens 212 focuses the portion of the first beam of blue light 112 reflected from the second mirror 210 through the input coupler 213 onto the laser gain element 214.

The first input coupler 213 may be, for example, a plane mirror or a reflective coating on a face of the first upconversion laser gain element 214 adjacent to the first focusing lens 212. The first input coupler 213 is transmissive at blue wavelengths and reflective at the green laser wavelength of the first upconversion laser gain element 214.

The first output coupler 216 may be, for example, a concave mirror that partially reflects and focuses the green light generated by the first upconversion laser gain element 214 back into the first upconversion laser gain element 214. The first output coupler 216 may also reflect the portion of the first beam of blue light 112 that is not absorbed by the first upconversion laser gain element 214 to increase optical efficiency and to avoid mixing blue light with the beam of green light 218.

The first upconversion laser gain element 214 may be, for example, a cylindrically shaped Pr^{3+} -doped YALO_3 (Pr:YALO) crystal having a length of about 1 cm and a diameter of about 0.6 cm. The first upconversion laser gain element 214 generates red light at a wavelength of about 644 nm and green light at a wavelength of about 520 nm from the portion of the first beam of blue light 112 reflected by the second beamsplitter 208 and the second mirror 210. Because the first input coupler 213 and the first output coupler 216 reflect green light in multiple passes through the first upconversion laser gain element

214, the first upconversion laser gain element 214 generates green light almost exclusively. The beam of green light 218 exits from the first output coupler 216.

The second focusing lens 220 focuses the
5 portion of the first beam of blue light 112 transmitted by the second beamsplitter 208 through the second input coupler 221 onto the second upconversion laser gain element 222. The second input coupler 221 may be, for example, a plane mirror or a reflective coating on a face
10 of the second upconversion laser gain element 222 adjacent to the second focusing lens 220. The second input coupler 221 transmits the portion of the first beam of blue light 112 transmitted by the second beamsplitter 208 and reflects red light generated by the second
15 upconversion laser gain element 222.

The second output coupler 224 may be, for example, a concave mirror that partially reflects and focuses the red light generated by the second
upconversion laser gain element 222 back into the second
20 upconversion laser gain element 222. The second output coupler 224 may also reflect blue light that is not absorbed by the second upconversion laser gain element 222 to increase optical efficiency and to avoid mixing blue light with the beam of red light 226.

The second upconversion laser gain element 222
may be, for example, a Pr^{3+} -doped YAlO_3 (Pr:YALO) crystal. The second upconversion laser gain element 222 generates red and green light from the beam of blue light 112. Because the second input coupler 221 and the second
25 output coupler 224 reflect red light in multiple passes through the second upconversion laser gain element 222, the second upconversion laser gain element 222 generates red light almost exclusively. The beam of red light 226 exits from the second output coupler 224.
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The optical modulators 250a, 250b, and 250c may be, for example, readily available acousto-optical

modulators optically coupled to the beam of red light 226, the beam of green light 218, and the second beam of blue light 206 respectively to vary the intensity of each RGB color. A wavelength dispersive device (not shown),
5 such as a diffraction grating or a prism, may be used to combine the beam of red light 226, the beam of green light 218, and the second beam of blue light 206 into a single beam of an RGB color, including white, according to well known techniques.

10 FIG. 3 is a diagram of an RGB light generator 300 with a single upconversion laser. Shown in FIG. 3 are a first beam of blue light 112, a beamsplitter 302, a second beam of blue light 304, a focusing lens 306, an input coupler 307, an upconversion laser gain element
15 308, a wavelength selective element 310, a first output coupler 312, a beam of red light 314, a second output coupler 316, and a beam of green light 318.

The beamsplitter 302 may be a 90%-10% beamsplitter similar to the beamsplitter 202 described
20 above for FIG. 2. The beamsplitter 302 splits the second beam of blue light 304 from the first beam of blue light 112 and transmits the greater portion of the blue light to the focusing lens 306. The focusing lens 306 focuses the first beam of blue light 112 through the input
25 coupler 307 onto the laser gain element 308.

The input coupler 307 may be, for example, a plane mirror or a reflective coating on a face of the upconversion laser gain element 308 adjacent to the focusing lens 306. The input coupler 307 transmits blue
30 light and reflects red and green light generated by the upconversion laser gain element 308.

The upconversion laser gain element 308 may be, for example, a Pr^{3+} -doped YAlO_3 (Pr:YALO) crystal that generates red and green light from blue light similar to
35 the upconversion laser gain element 214 or 222 in FIG. 2. Because the input coupler 307 and the output couplers 312

and 316 reflect both red and green light in multiple passes through the upconversion laser gain element 308, the upconversion laser gain element 308 generates red and green light almost exclusively.

5 The wavelength selective element 310 may be, for example, a flat quartz plate coated with a dichroic coating that is commercially available from numerous suppliers, or a prism. The wavelength selective element 310 directs the red light generated by the upconversion
10 laser gain element 308 to the first output coupler 312 and the green light generated by the upconversion laser gain element 308 to the second output coupler 316.

 The first output coupler 312 may be, for example, a concave mirror that is partially reflective,
15 for example, between 10% and 99% reflective, at the red laser wavelength of the laser gain element 308. The first output coupler 312 partially reflects and focuses the red light generated by the upconversion laser gain element 308 back into the upconversion laser gain element
20 308, and the output beam of red light 314 exits from the first output coupler 312.

 The second output coupler 316 may be, for example, a concave mirror that is partially reflective, for example, between 10% and 99% reflective, at the green
25 laser wavelength of the laser gain element 308. The second output coupler 316 partially reflects and focuses the green light generated by the upconversion laser gain element 308 back into the upconversion laser gain element 308, and the beam of green light 318 exits from the
30 second output coupler 316.

 Optical modulators (not shown) similar to optical modulators 250a, 250b, and 250c described above for FIG. 2 may be optically coupled to the beam of red light 314, the beam of green light 318, and the second
35 beam of blue light 304 to vary the intensity of each RGB color according to well known techniques.

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FIG. 4 is a diagram of an RGB light generator 400 for generating beams of red, green, and blue light that are collinear. Shown in FIG. 4 are a first beam of blue light 112, a focusing lens 402, an input coupler 403, an upconversion laser gain element 404, an output coupler 406, and collinear beams 408 of blue light, red light, and green light.

The focusing lens 402 focuses the first beam of blue light 112 through the input coupler 403 onto the laser gain element 404. The input coupler 403 may be, for example, a plane mirror or a reflective coating on a face of the upconversion laser gain element 404 adjacent to the focusing lens 402. The input coupler 403 transmits the input beam of blue light 112 and reflects red and green light generated by the upconversion laser gain element 404.

The upconversion laser gain element 404 may be, for example, a Pr^{3+} -doped YALO_3 (Pr:YALO) crystal that generates red and green light from the first beam of blue light 112 similar to the upconversion laser gain element 308 in FIG. 3. Because the input coupler 403 and the output coupler 406 are reflective at both the red and green wavelengths, the upconversion laser gain element 404 generates both red and green light.

The output coupler 406 may be, for example, a concave mirror that is partially reflective, for example, between 10% and 99% reflective, at the red and green laser wavelengths of the laser gain element 404, and is also highly transmissive at the blue wavelength. This may be accomplished using a dichroic coating on the concave mirror according to techniques well known in the art. The output coupler 406 partially reflects and focuses light at the red and green laser wavelengths back into the upconversion laser gain element 404, and the collinear beam of blue, red, and green light 408 exits from the output coupler 406.

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FIG. 5 is a diagram of an RGB light generator 500 for generating separate beams of red, green, and blue light. The RGB light generator 500 combines the separate beams to form a collinear beam of combined red, green, and blue light. Shown in FIG. 5 are a first beam of blue light 112, a focusing lens 502, an input coupler 503, an upconversion laser gain element 504, a first wavelength selective element 506, a first output coupler 508, a beam of red light 510, a second output coupler 512, a beam of green light 514, a beam of blue light 516, a second wavelength selective element 518, and a collinear beam of combined red, green, and blue light 520.

The focusing lens 502 focuses the first beam of blue light 112 through the input coupler 503 onto the laser gain element 504. The input coupler 503 may be, for example, a plane mirror or a reflective coating on a face of the upconversion laser gain element 504 adjacent to the focusing lens 502. The input coupler 503 transmits blue light and reflects red and green light generated by the upconversion laser gain element 504.

The upconversion laser gain element 504 may be, for example, a Pr^{3+} -doped YALO_3 (Pr:YALO) crystal that generates red and green light from blue light similar to the upconversion laser gain element 308 in FIG. 3. Because the input coupler 503 and the first output coupler 508 reflect red light, and because the input coupler 503 and the second output coupler 512 reflect green light, the upconversion laser gain element 504 generates red and green light.

The first wavelength selective element 506 and the second wavelength selective element 518 may be, for example, a diffraction grating, a dichroic mirror, or a prism. The wavelength selective element 506 separates the red light and the green light generated by the upconversion laser gain element 504 and the portion of

the first beam of blue light 112 that is not absorbed by the upconversion laser gain element 504.

The first output coupler 508 may be, for example, a concave mirror that is partially reflective, for example, between 10% and 99% reflective, at the red laser wavelength of the laser gain element 504. The first output coupler 508 partially reflects and focuses light at the red laser wavelength back into the upconversion laser gain element 504, and the beam of red light 510 exits from the first output coupler 508.

The second output coupler 512 may be, for example, a concave mirror that is partially reflective, for example, between 10% and 99% reflective, at the green laser wavelength of the laser gain element 504. The second output coupler 512 partially reflects and focuses green light back into the upconversion laser gain element 504, and the beam of green light 514 exits from the second output coupler 512.

Optical modulators (not shown) may be optically coupled to the beam of red light 510, the beam of green light 514, and the beam of blue light 516 to vary the intensity of each color as described above for FIG. 2 according to well known techniques.

The second wavelength selective element 518 combines the beam of red light 510, the beam of green light 514, and the second beam of blue light 516 to form the collinear beam of combined red, green, and blue light 520. The color of the collinear beam of combined red, green, and blue light 520 may be selected by varying the intensity of each color to generate any color, including white.

The RGB light generator embodied in FIGS. 2, 3, 4, and 5 may be made entirely from solid state components as described above to generate light beams of red, green, blue, white, and any other color or combination of colors for a variety of applications including color displays

requiring an RGB generator that is light, portable, and shock-resistant.

While the invention herein disclosed has been described by means of specific embodiments and
5 applications thereof, other modifications, variations, and arrangements of the present invention may be made in accordance with the above teachings other than as specifically described to practice the invention within the spirit and scope defined by the following claims.

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